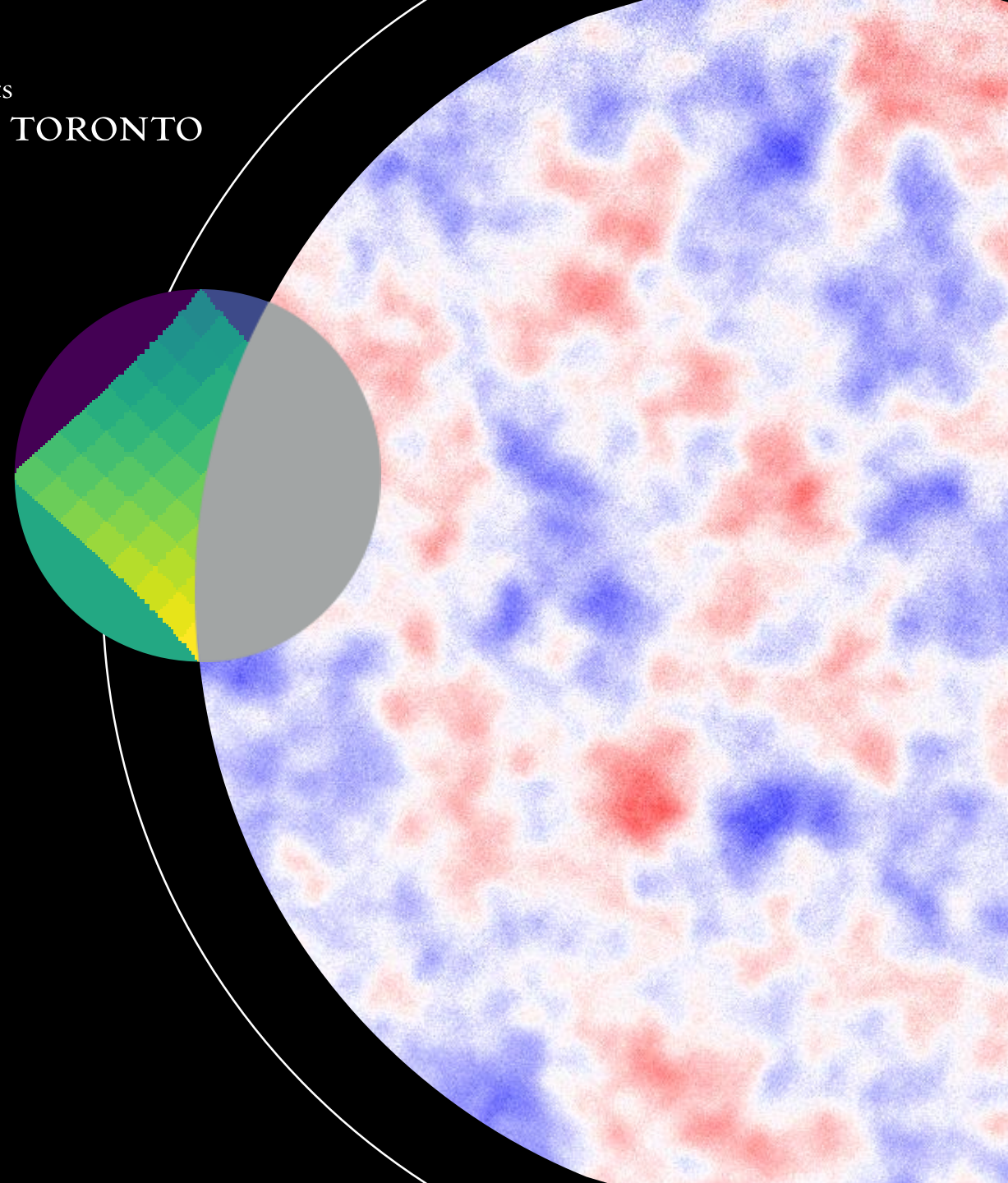




Small Scale CMB Lensing with Local Map-Space Statistics

Victor Carl Chan
Renée Hložek (Dunlap)
Alex van Engelen (CITA)
Joel Meyers (SMU)

The CMB in HD: the low noise high-resolution frontier



CMB lensing at small angular scales ($\ell \gg 3000$)

$$T_{lens}(\hat{n}) \approx T_0(\hat{n}) + \vec{\nabla} T_0(\hat{n}) \cdot \vec{\nabla} \phi$$

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Diffusion Damping

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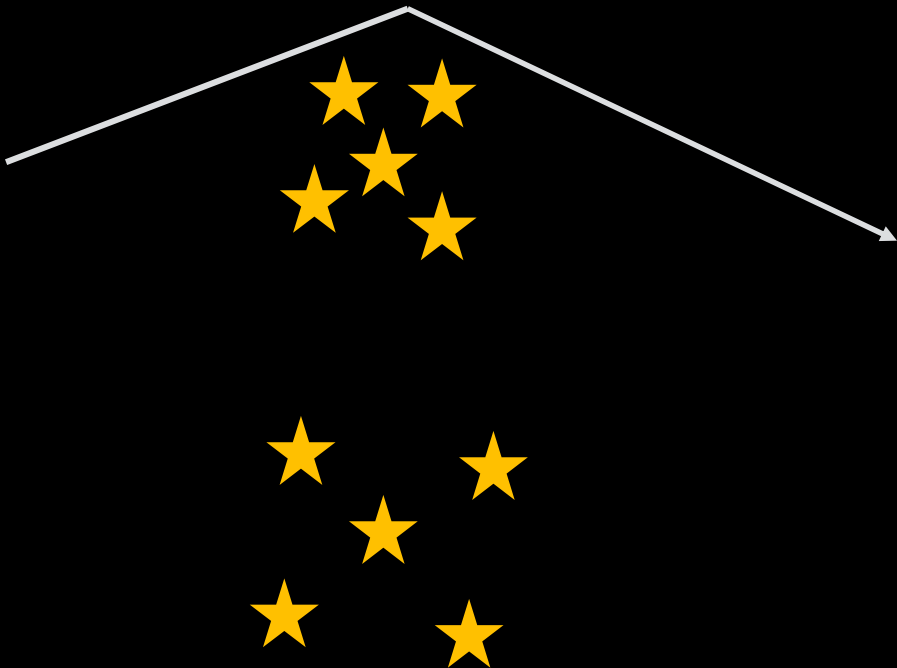
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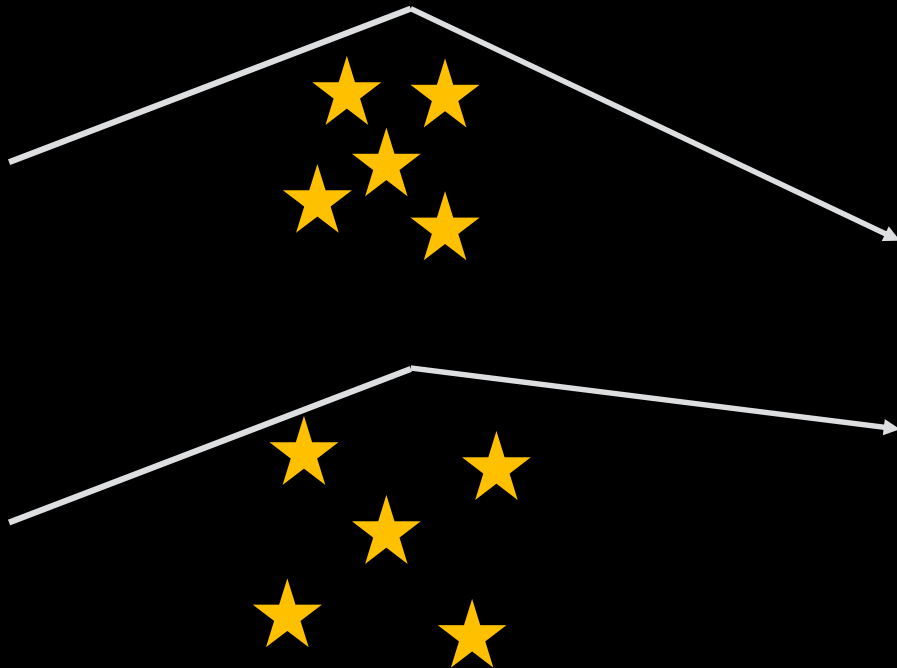
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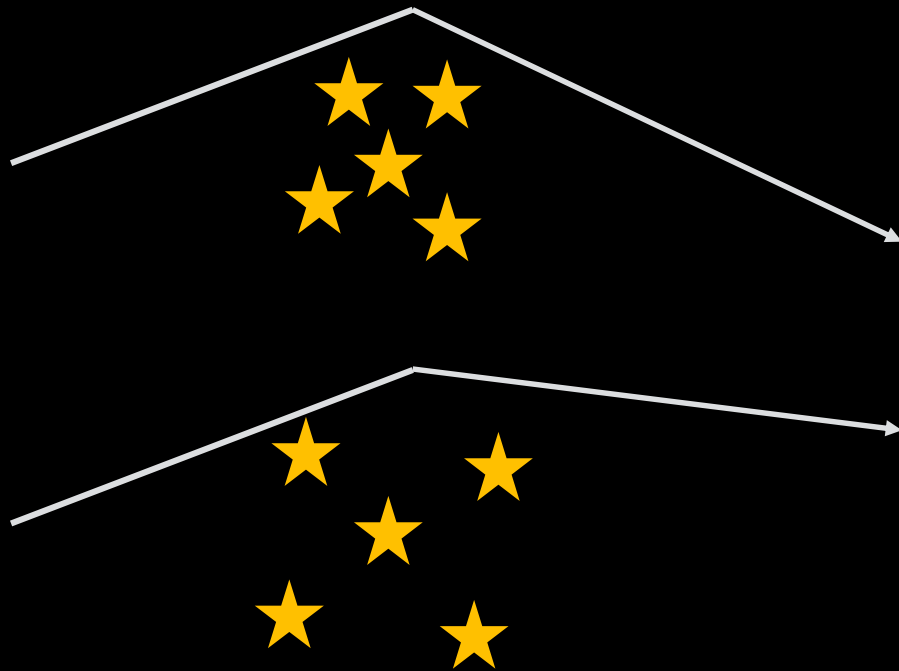
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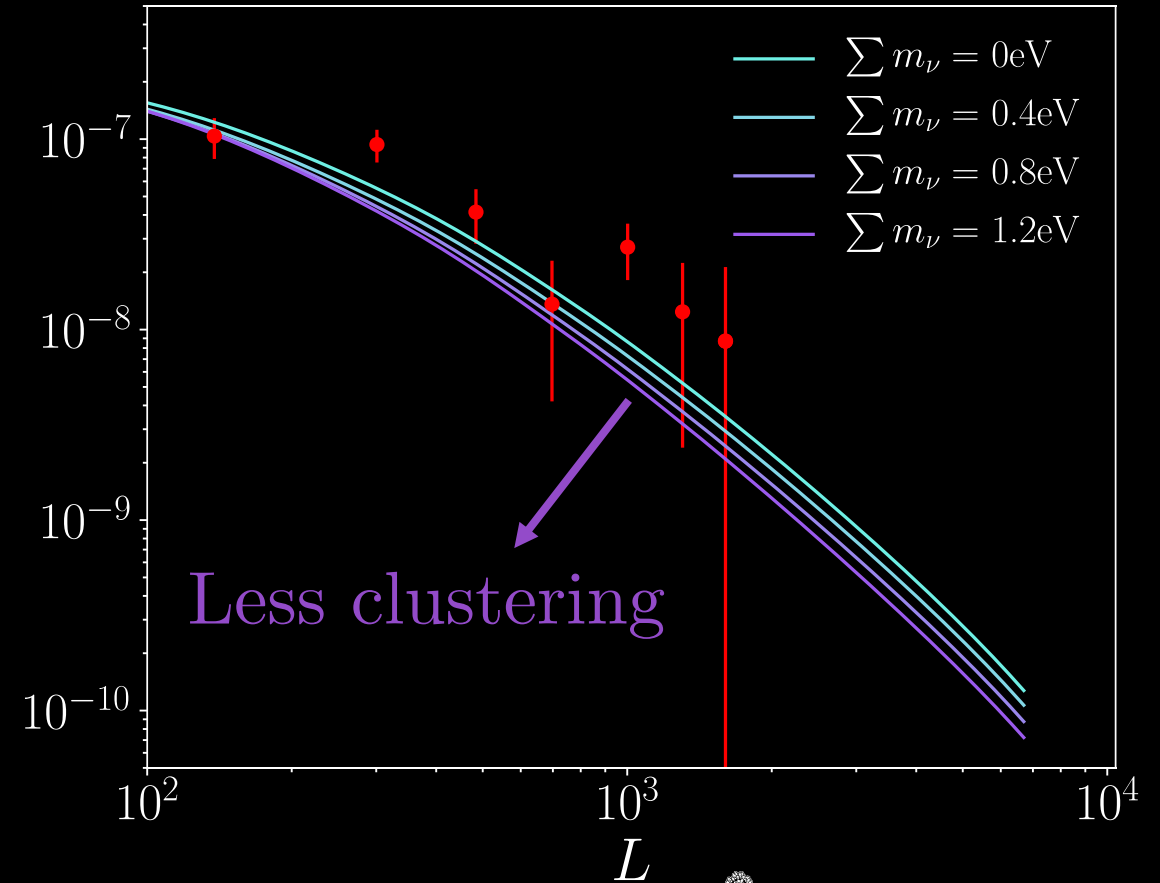


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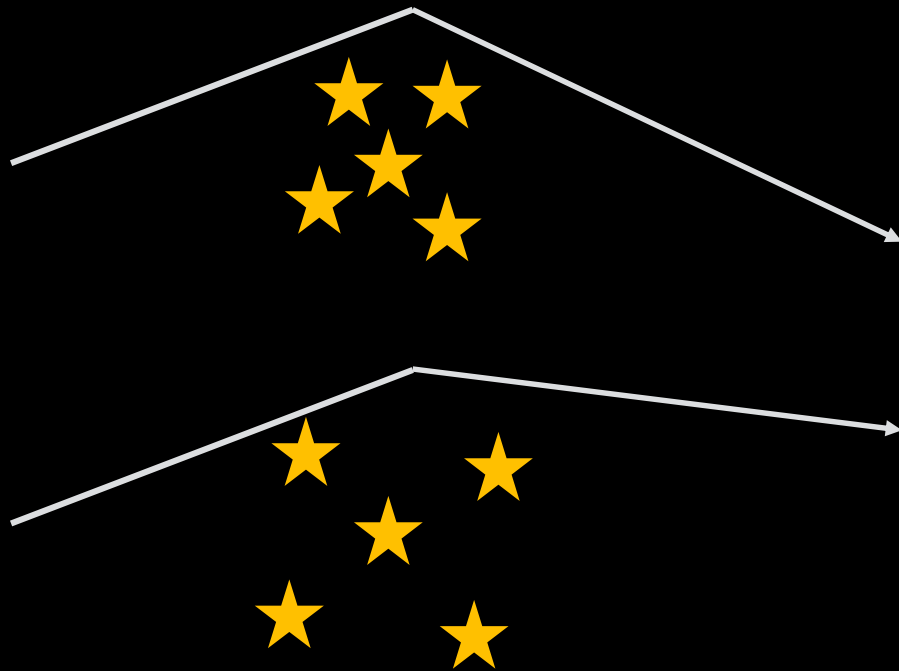


Lensing Power
 $C_L^{kk} = [L(L+1)]^2 C_L^{\phi\phi} / 4$



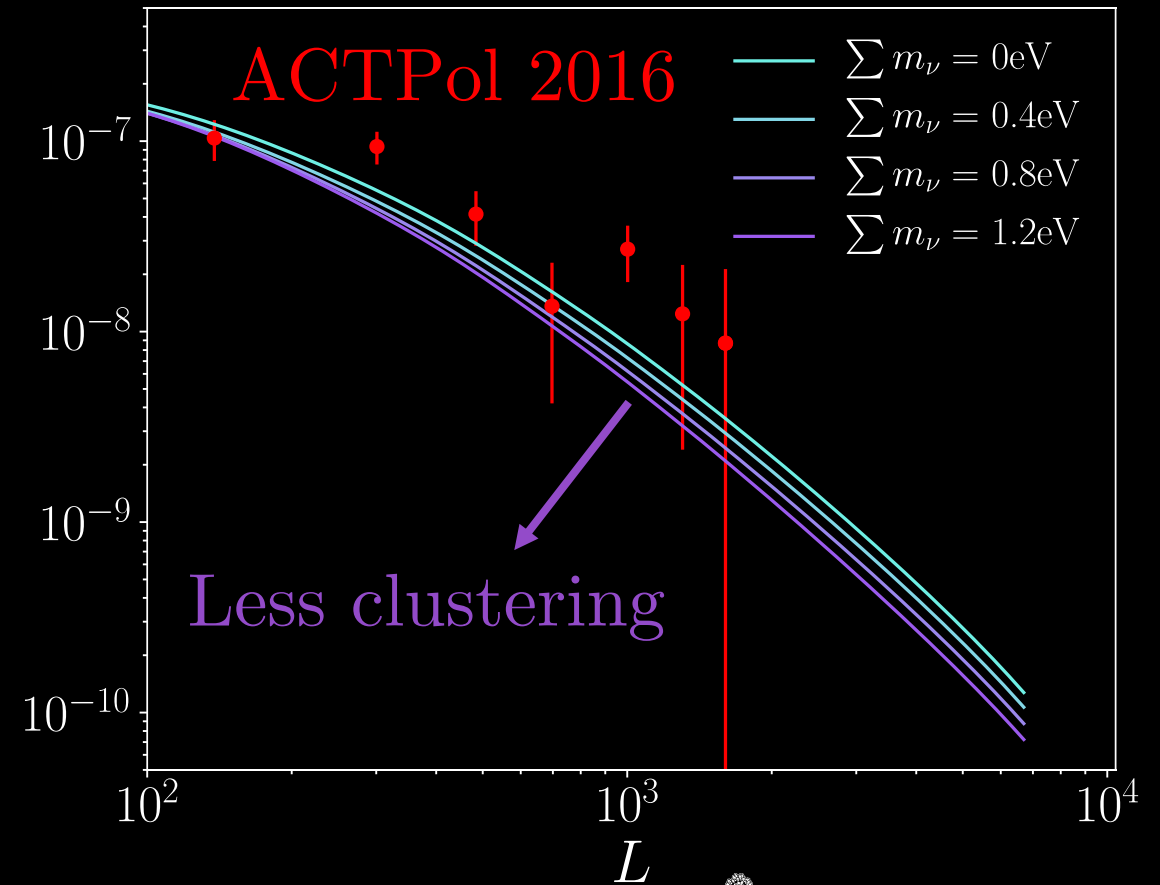
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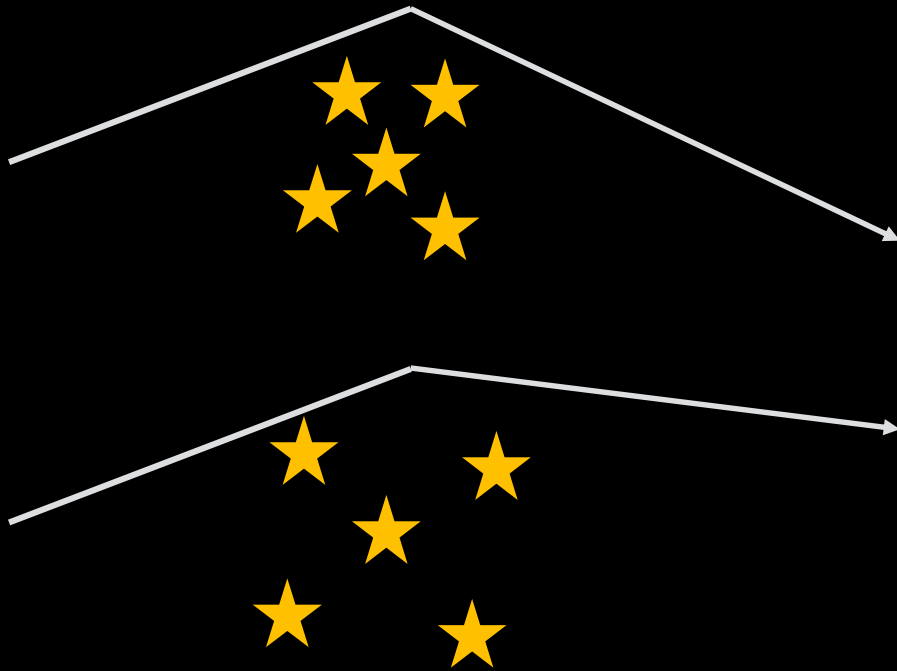
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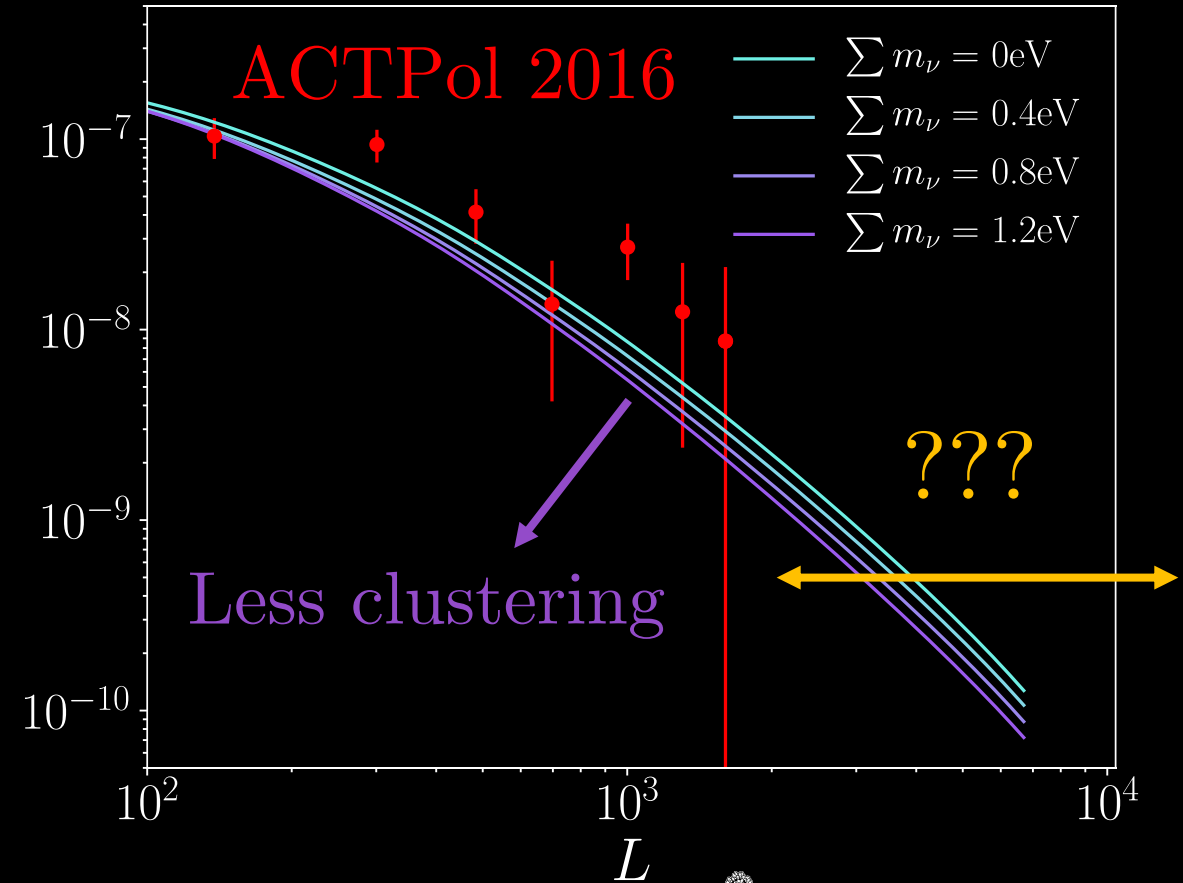
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Taking advantage of lensing dominated scales

$$\tilde{T}^{SS} \approx \vec{\nabla} T \cdot \vec{\nabla} \phi$$

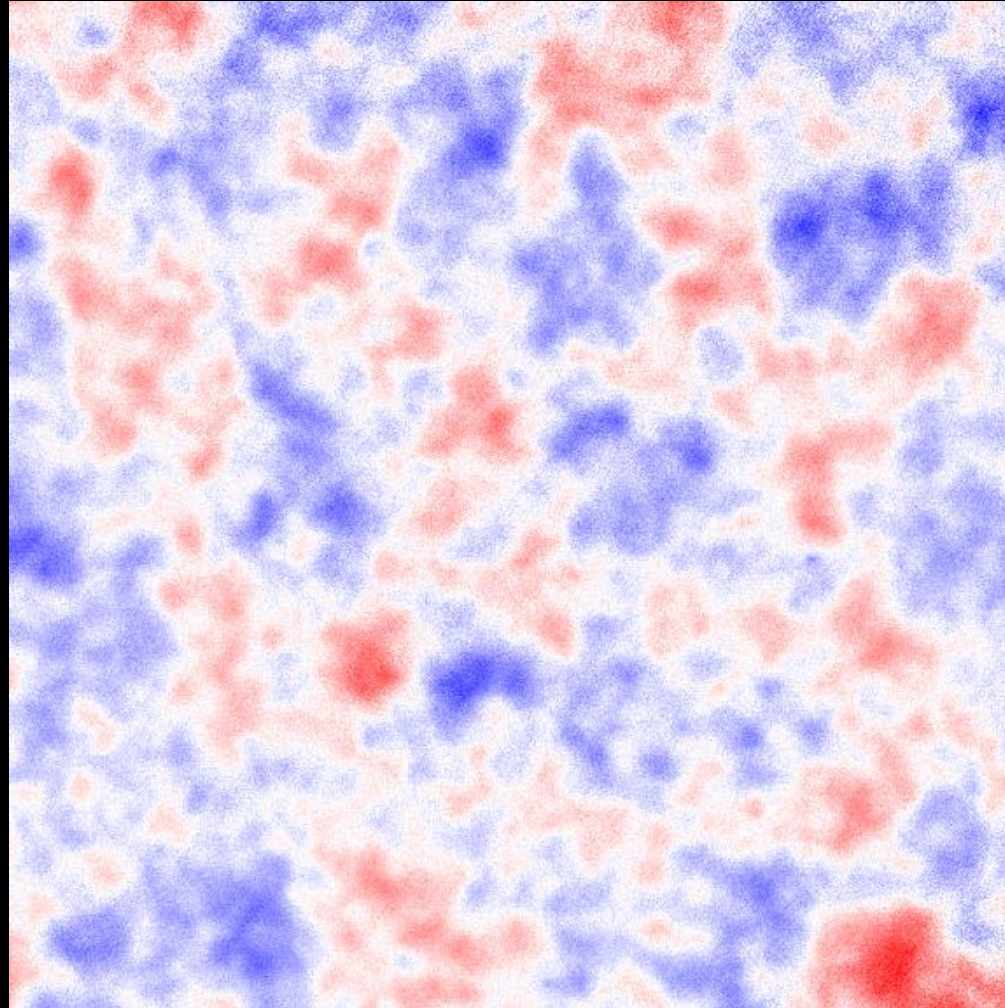
Taking advantage of lensing dominated scales $\tilde{T}^{SS} \approx \vec{\nabla} T \cdot \vec{\nabla} \phi$

Reconstruct lensing potential?

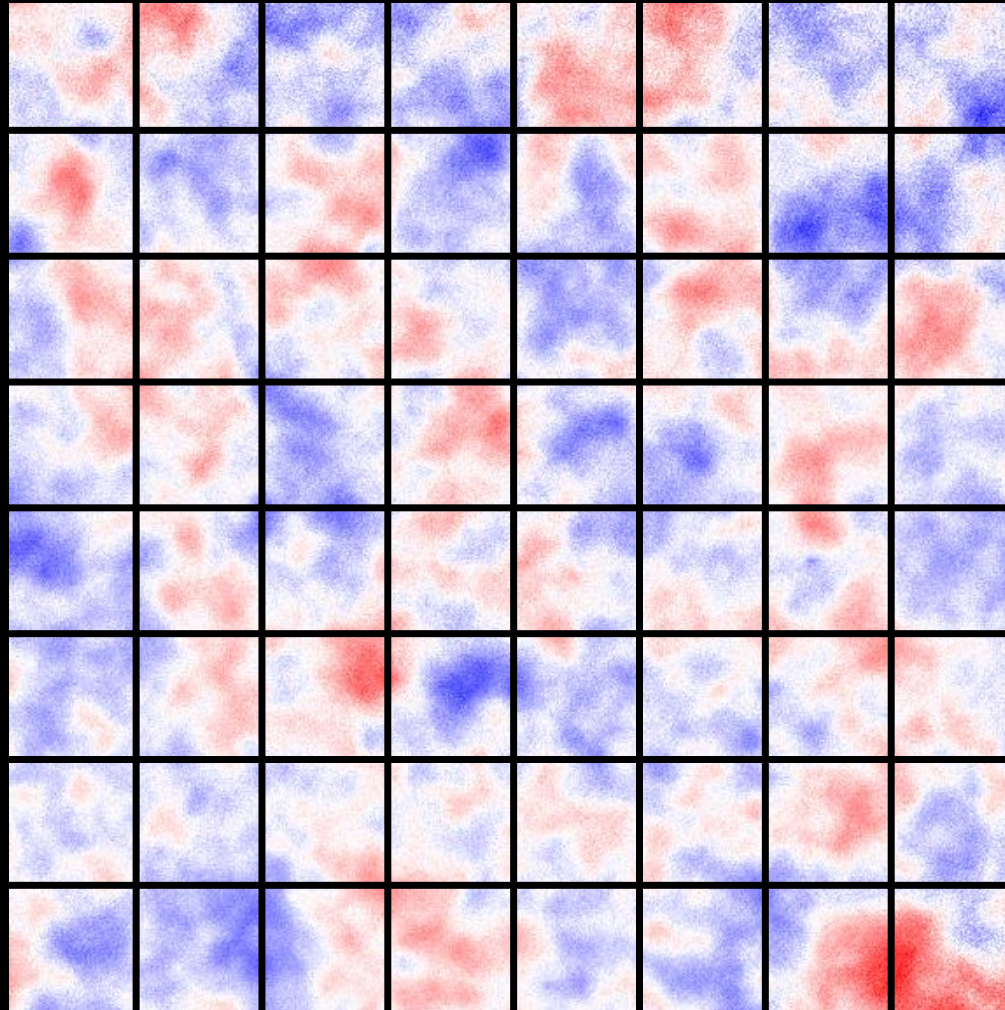
$$\nabla \phi \approx T / \nabla T$$

See Simone/Blake!

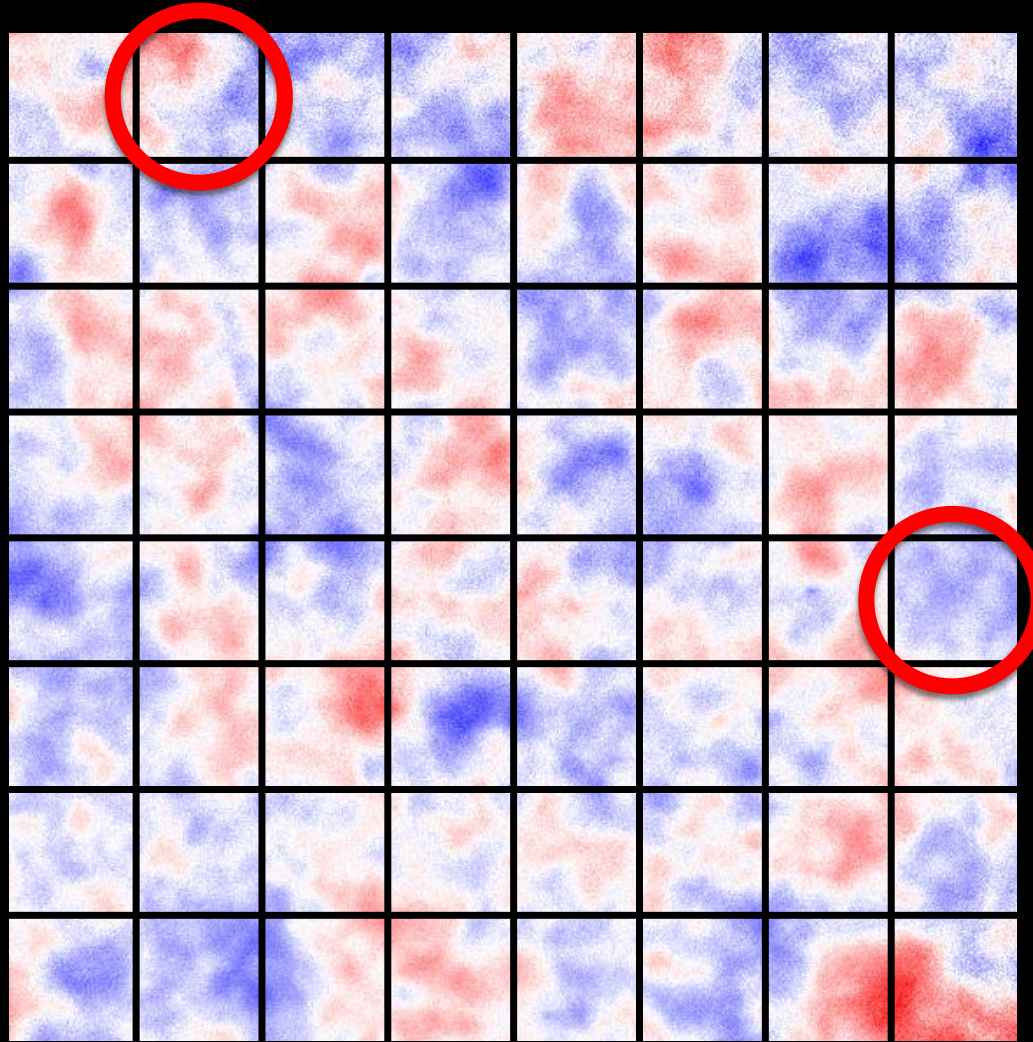
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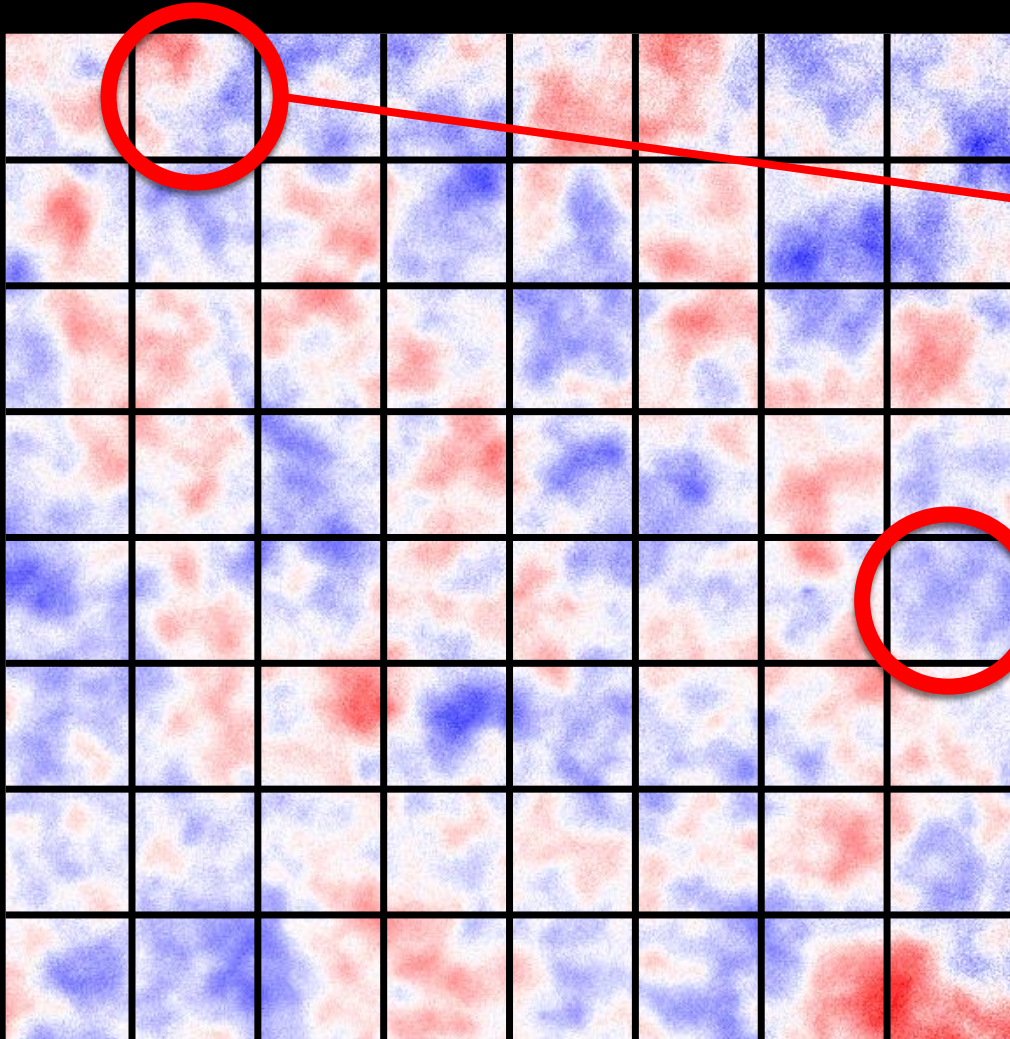


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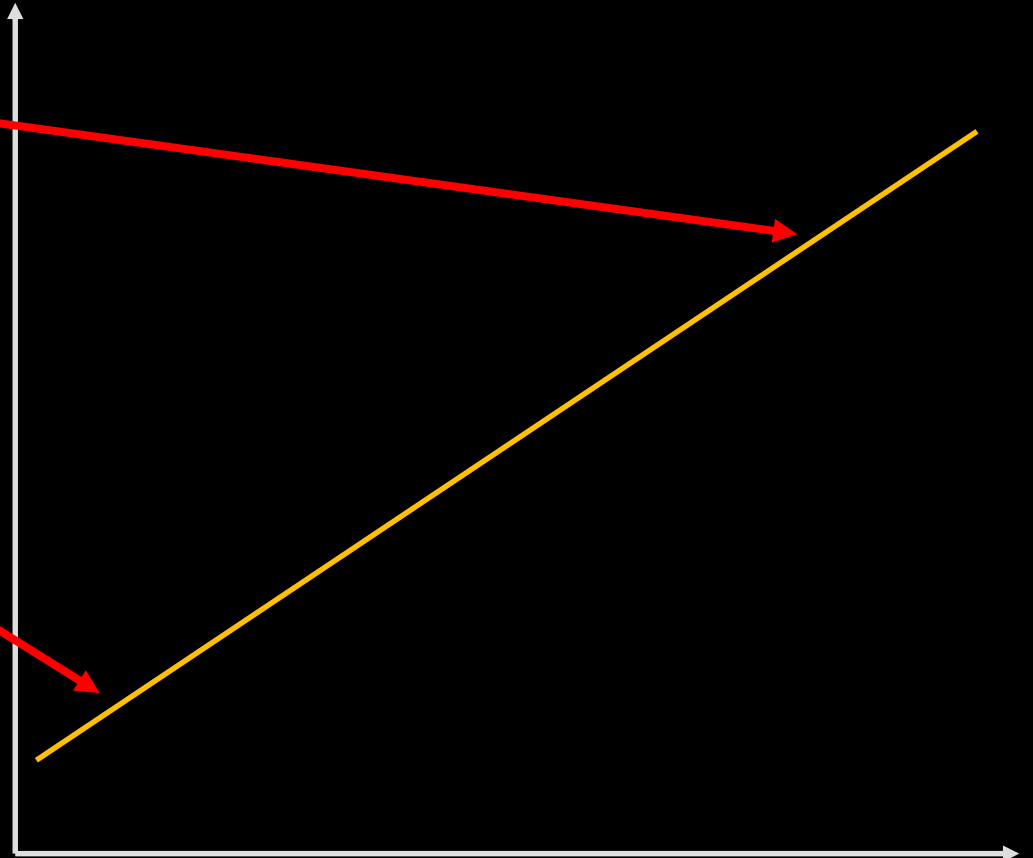


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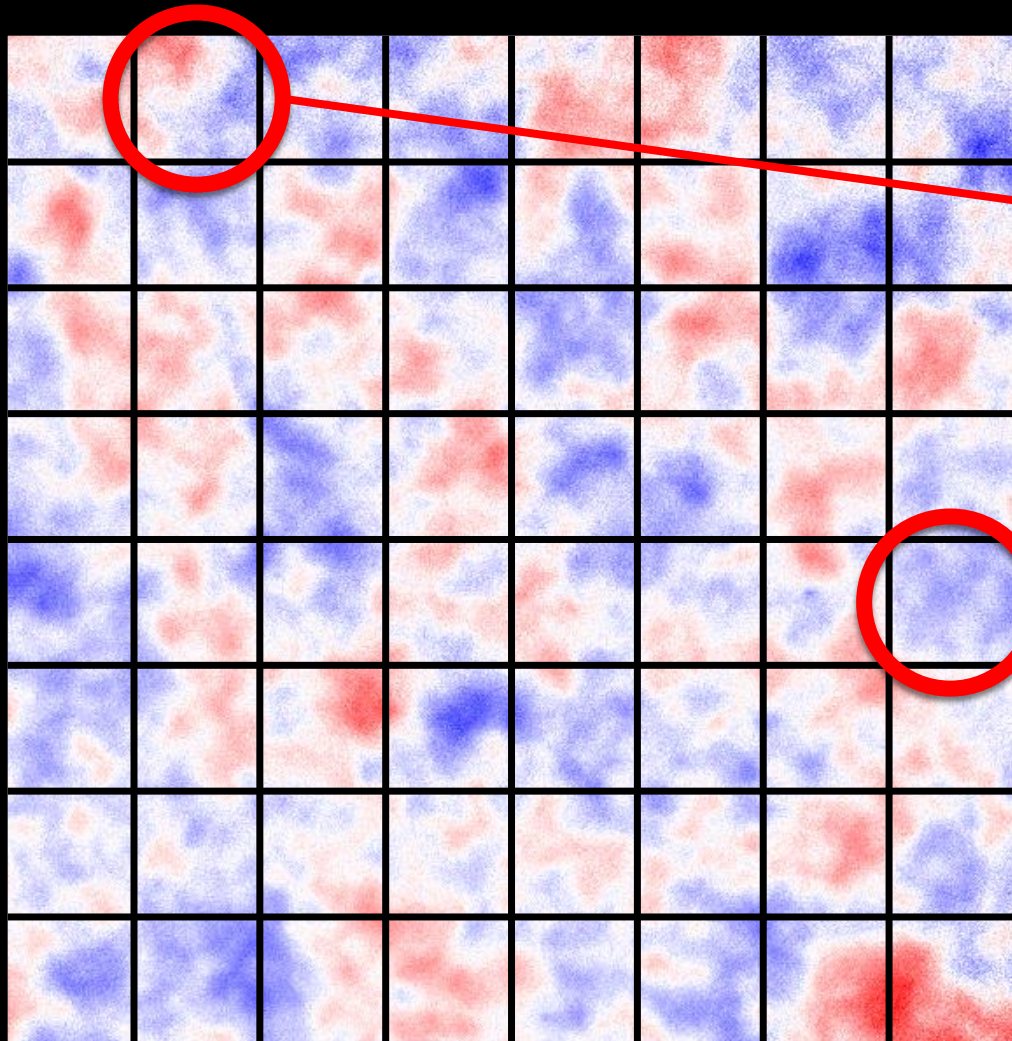


T_{SS}^2



$|\nabla T|^2$

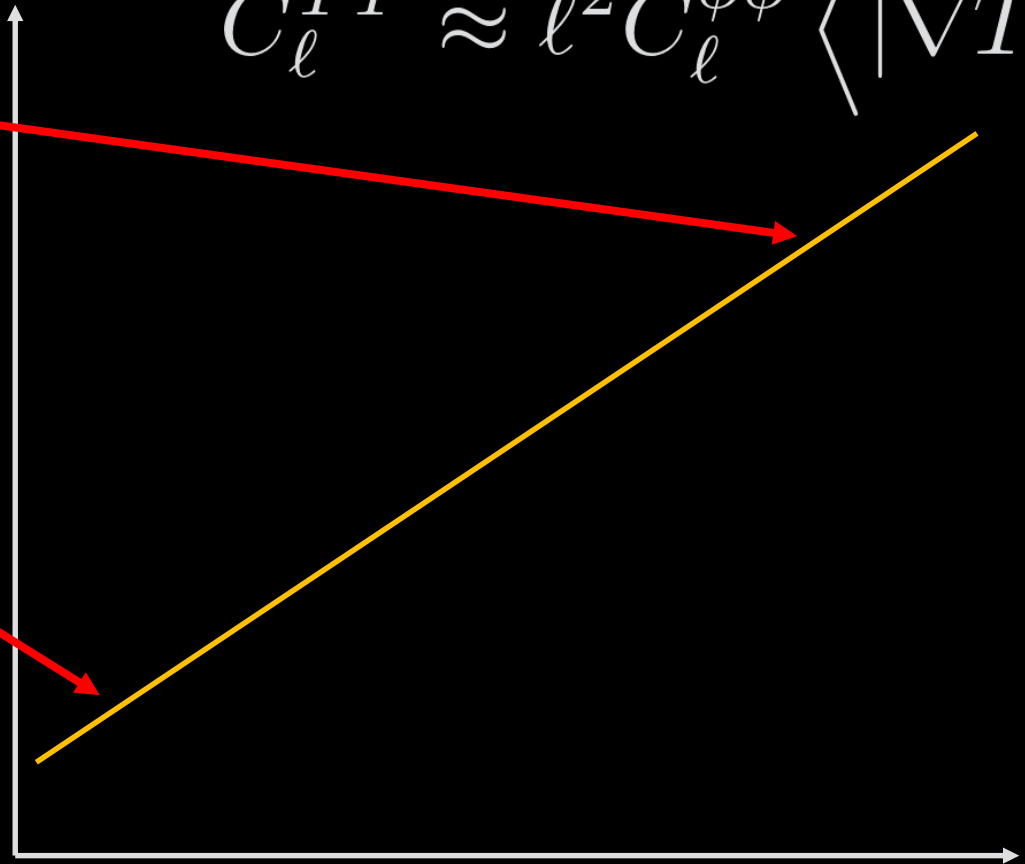
Taking advantage of lensing dominated scales



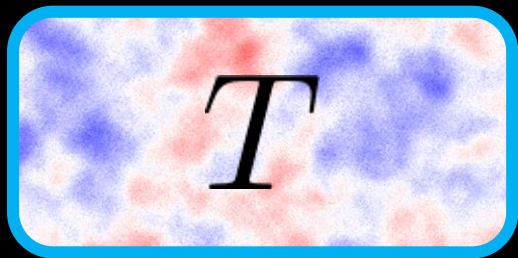
T_{SS}^2

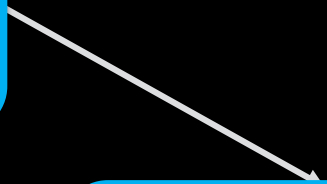
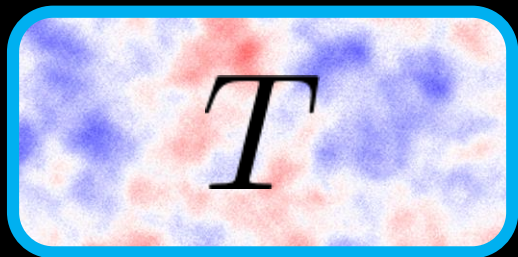
$$\tilde{T}^{SS} \approx \vec{\nabla} T \cdot \vec{\nabla} \phi$$

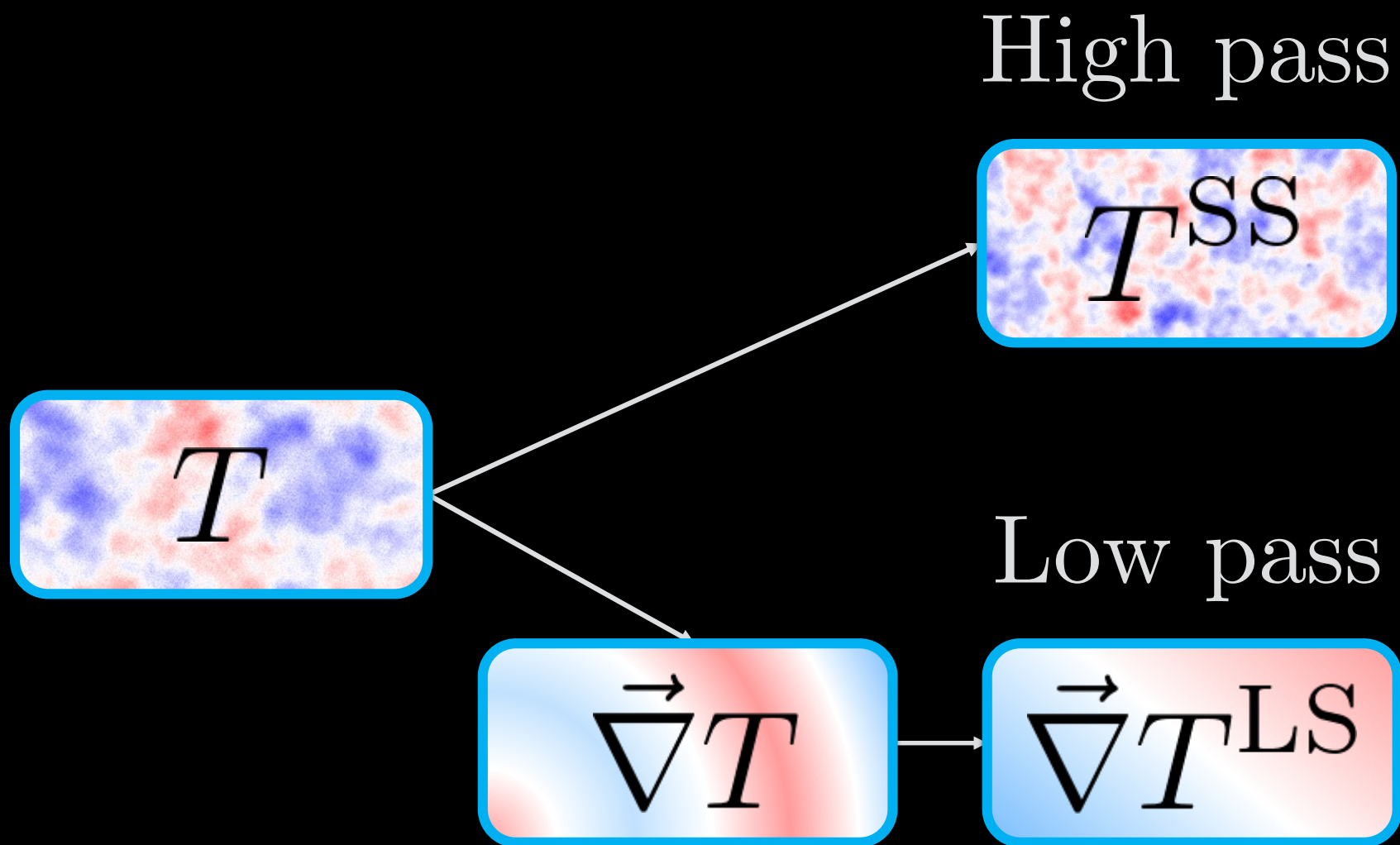
$$\tilde{C}_\ell^{TT} \approx \ell^2 C_\ell^{\phi\phi} \langle |\nabla T|^2 \rangle$$



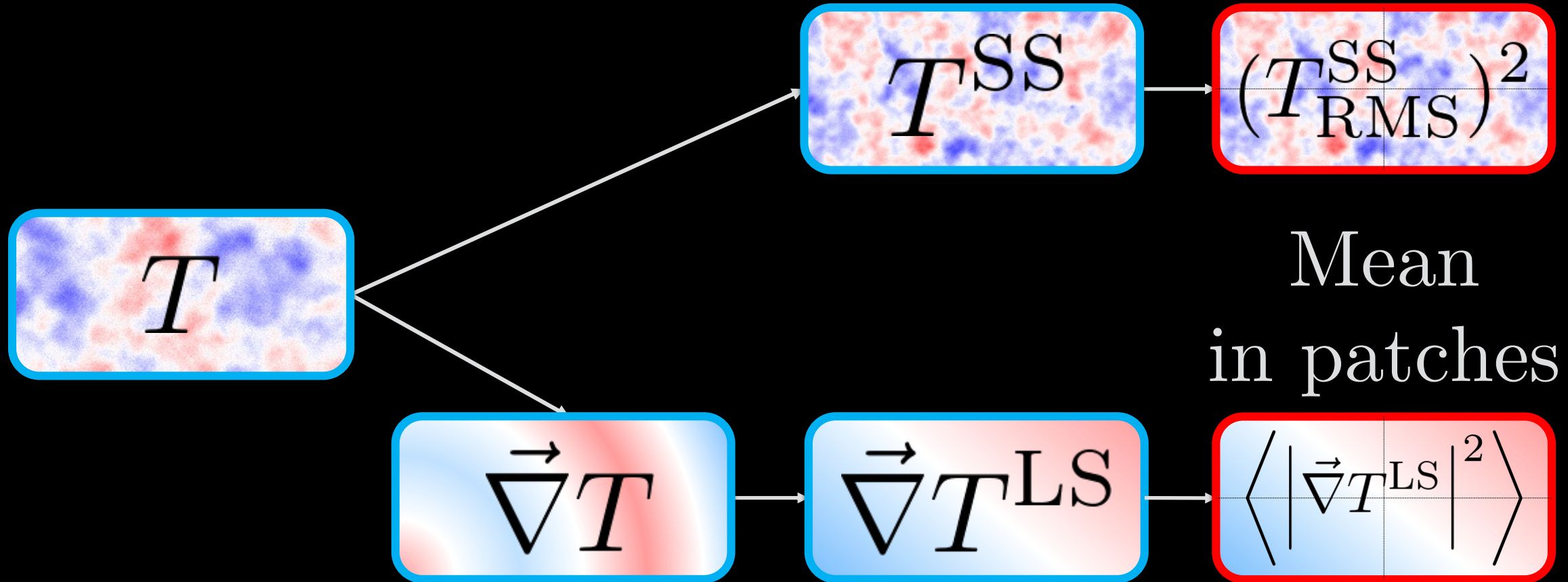
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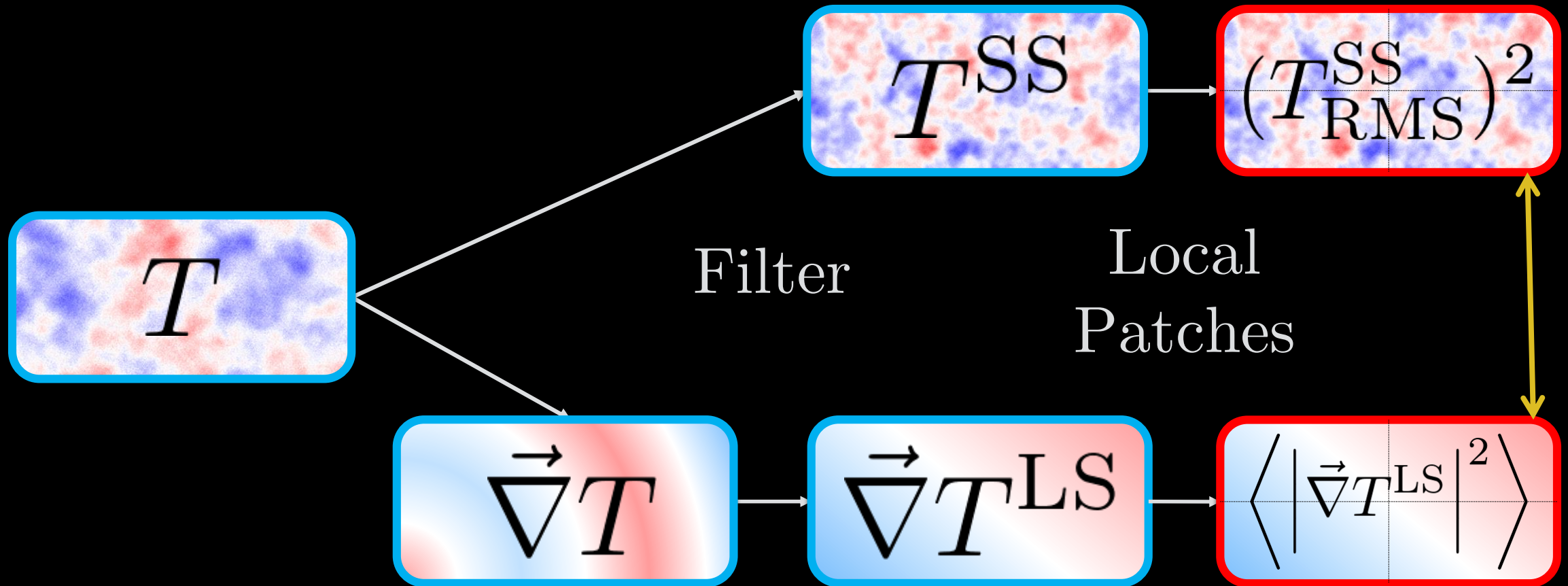
Variance
in patches



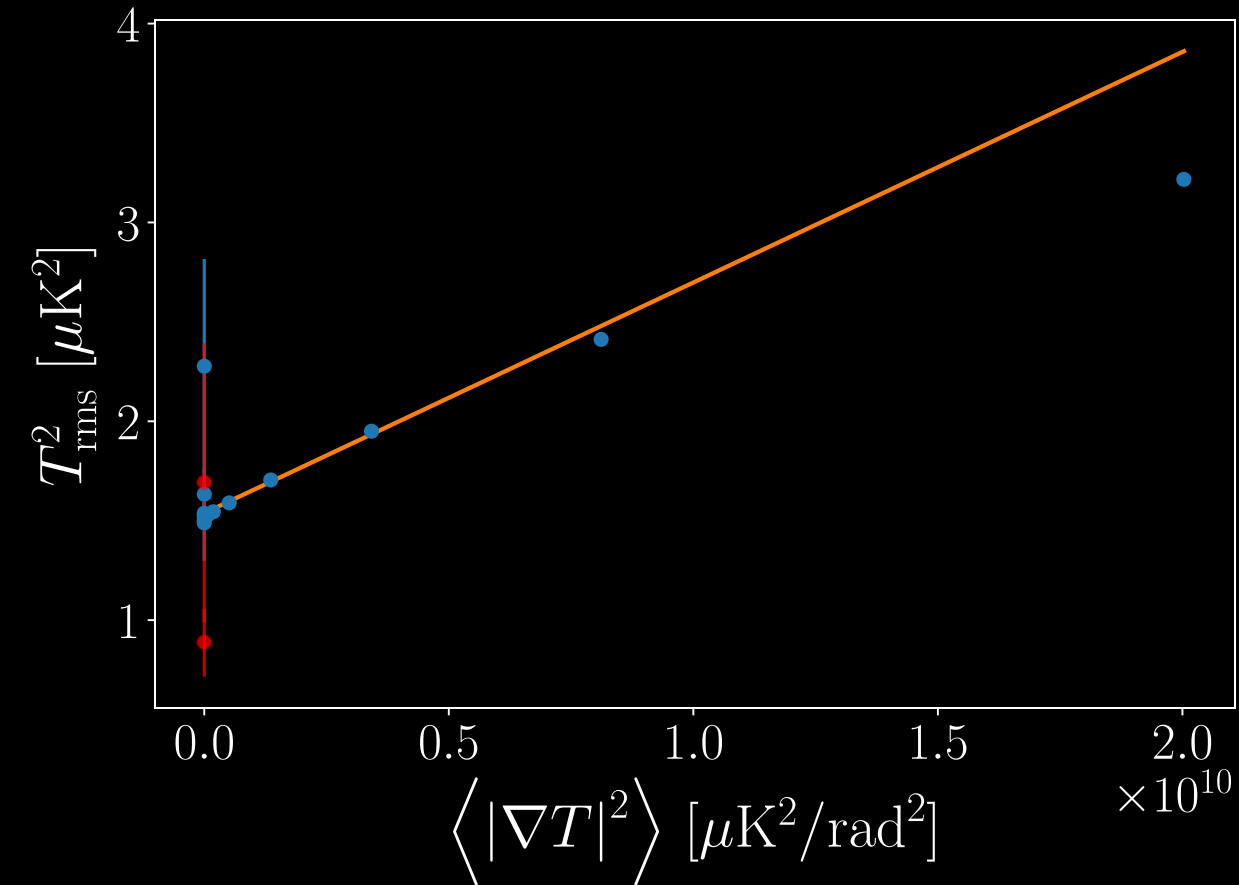
Mean
in patches

High Resolution

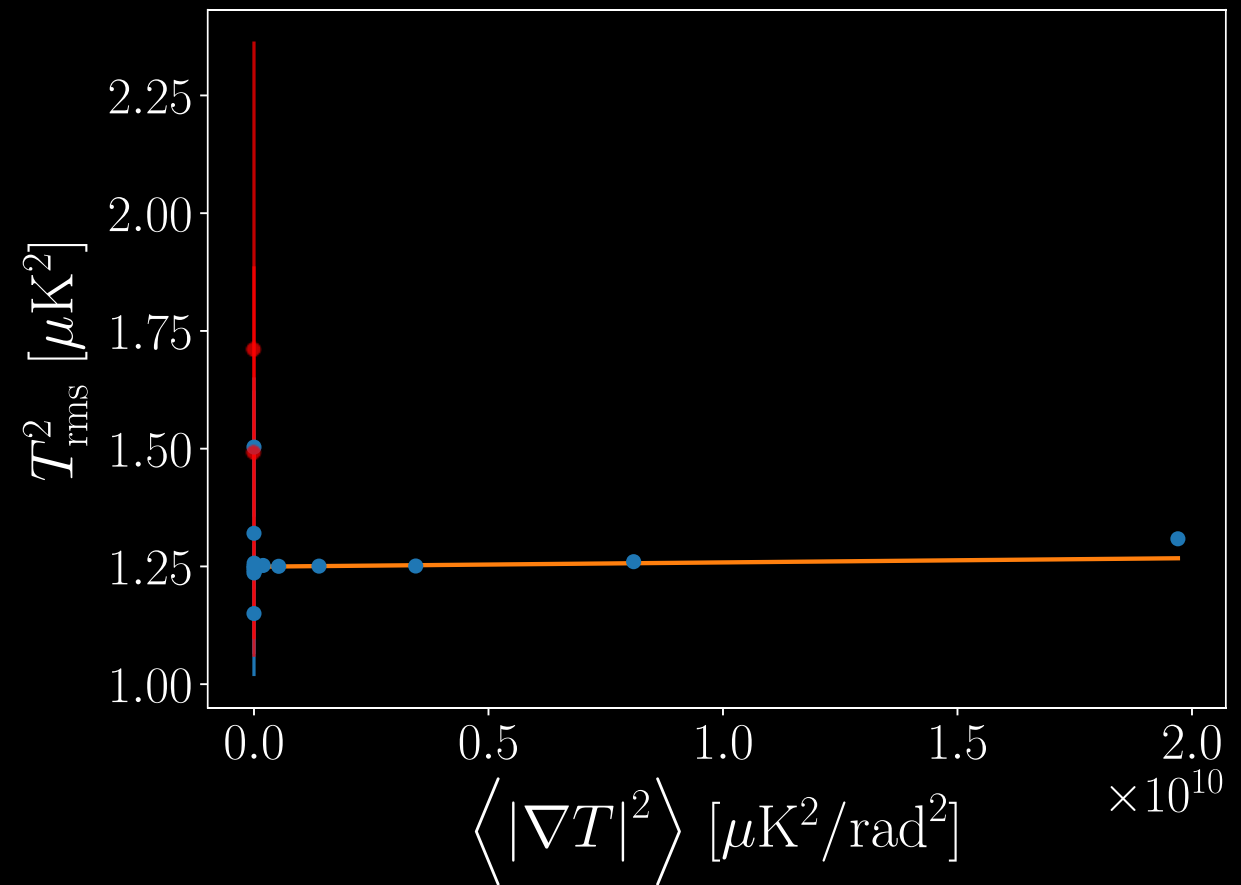
Lower Res



Lensed Map

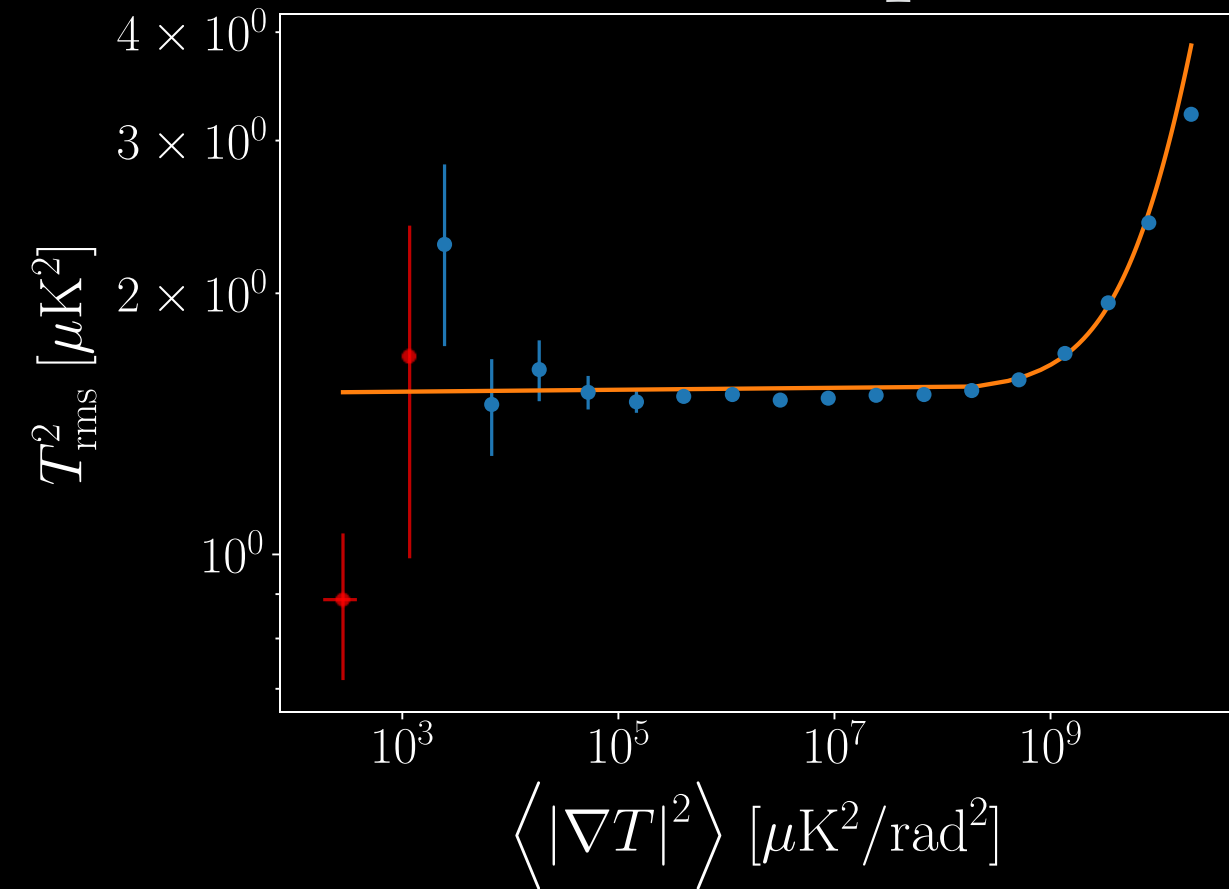


Unlensed Map

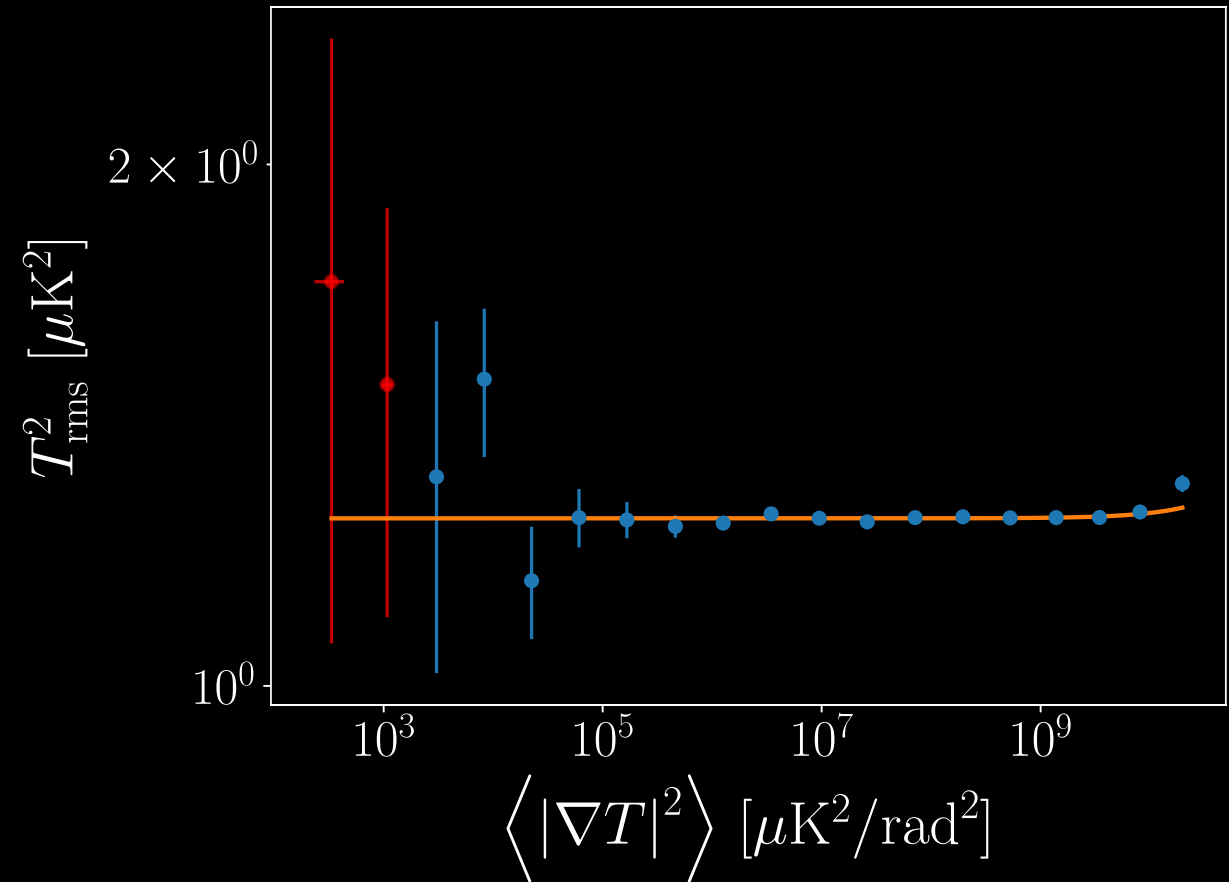


Log-space

Lensed Map

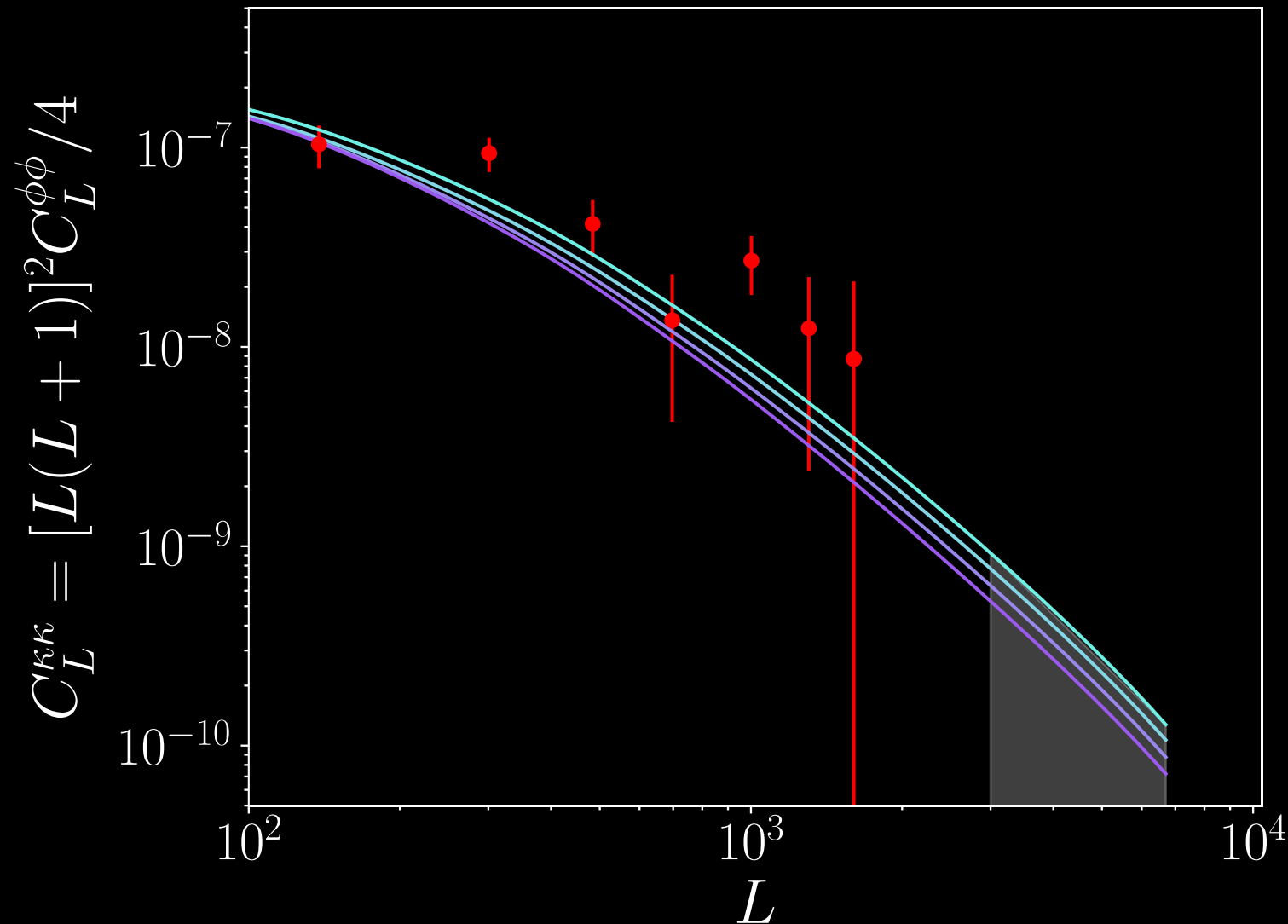


Unlensed Map



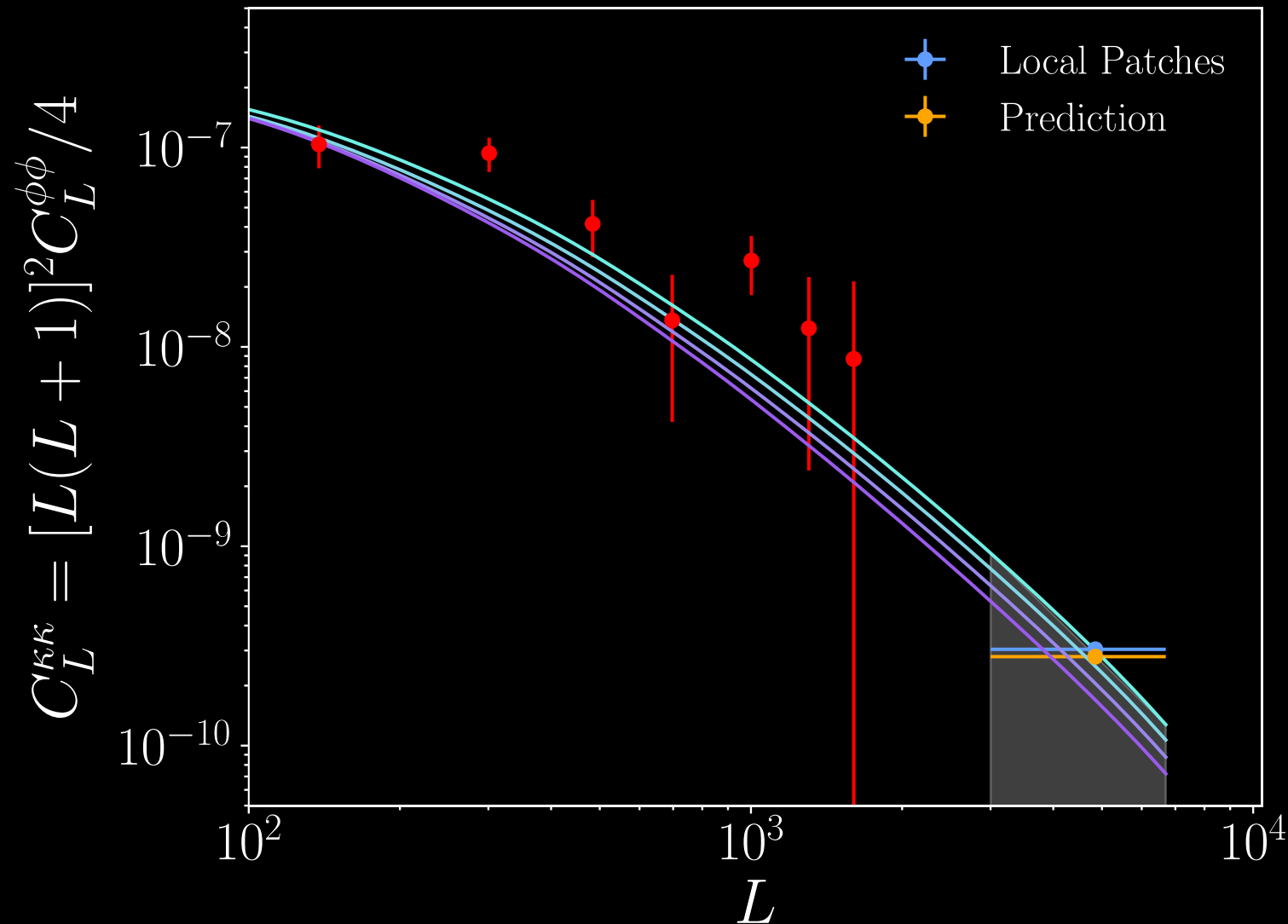
Ability to constrain small scale lenses

$$\tilde{C}_\ell^{TT} \approx \ell^2 C_\ell^{\phi\phi} \langle |\nabla T|^2 \rangle$$



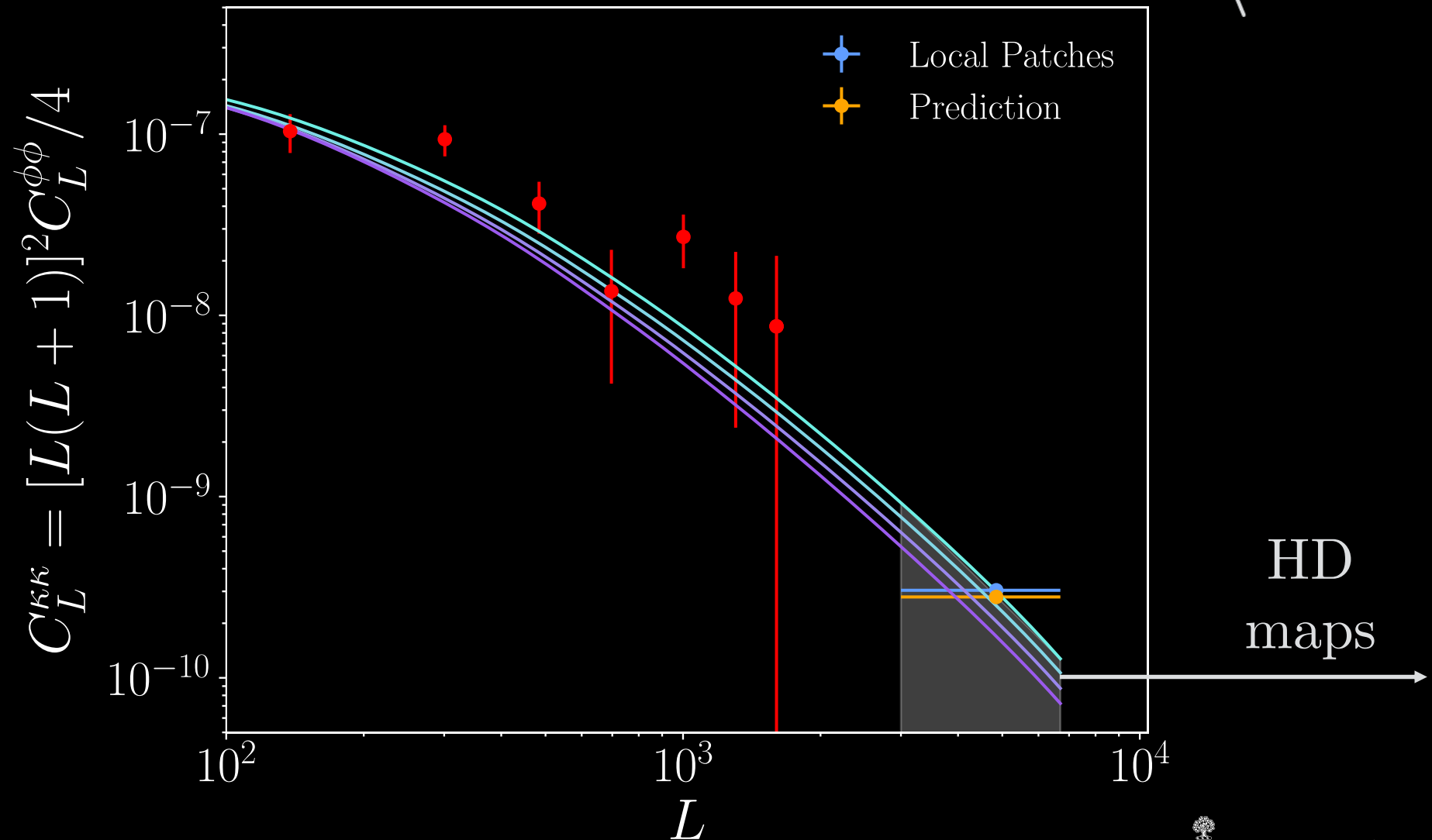
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Gradient direction?

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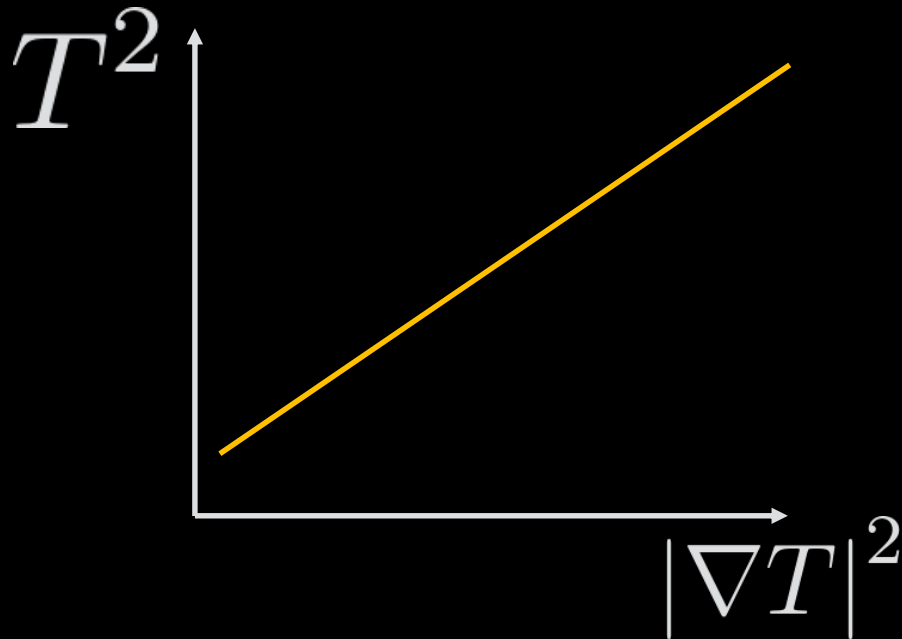
See Simone/Blake

Adding kSZ at small scales

$$\tilde{T}_{SS} \approx \vec{\nabla} T \cdot \vec{\nabla} \phi + \sum_z \tau_z v_{r,z}$$

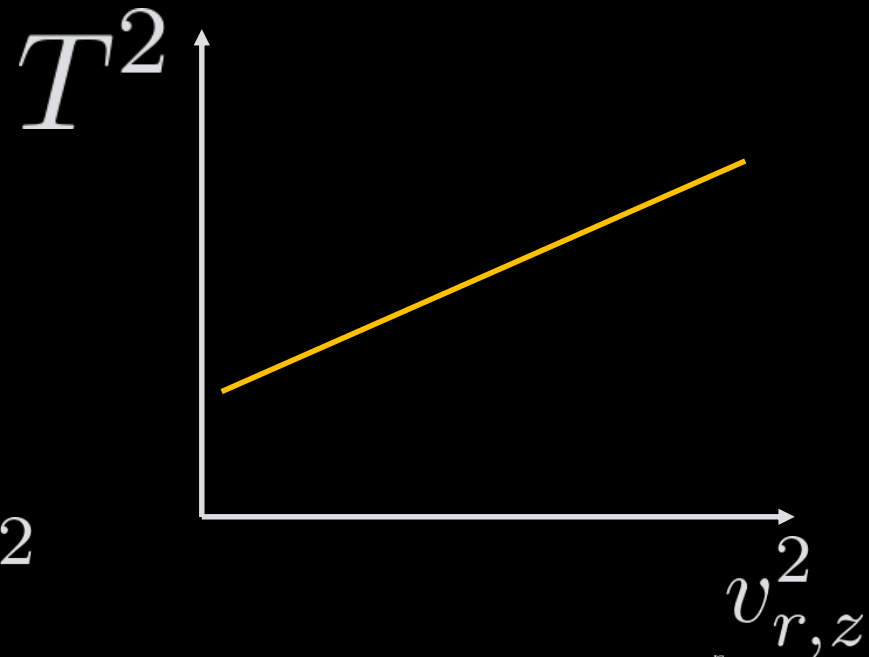
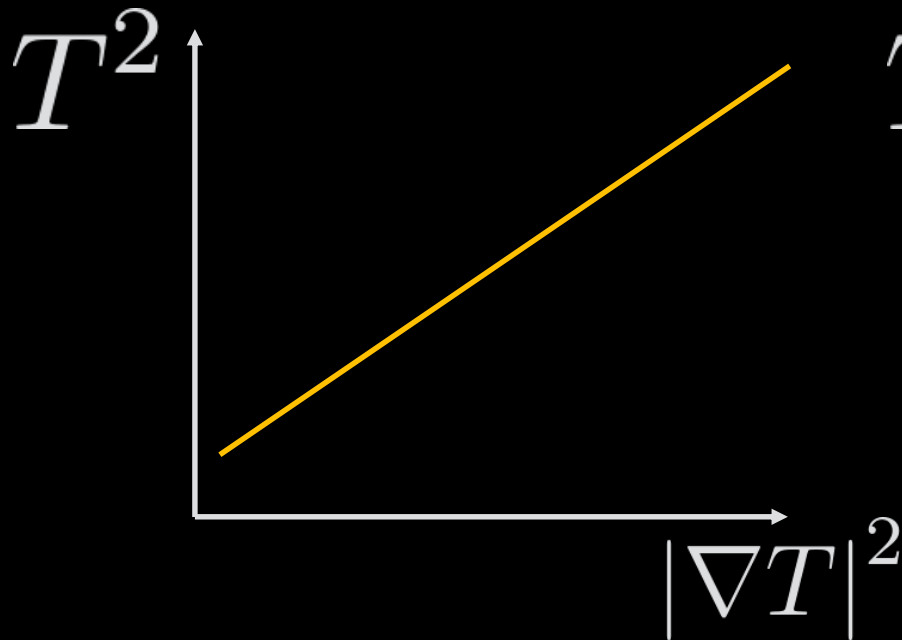
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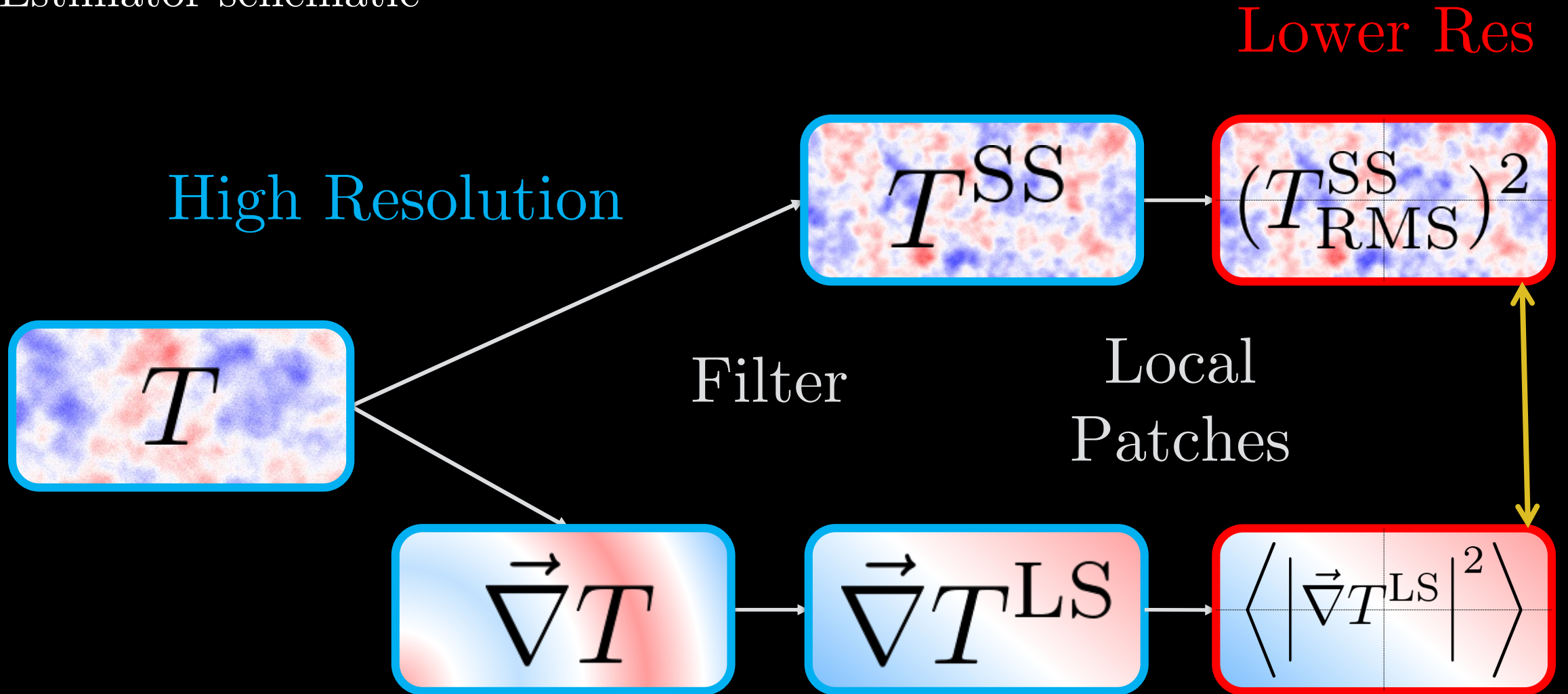
Adding kSZ at small scales

$$\tilde{T}_{SS} \approx \underbrace{\vec{\nabla} T \cdot \vec{\nabla} \phi}_{\text{CMB}} + \underbrace{\sum_z \tau_z v_{r,z}}_{\text{kSZ}}$$



Thank you!

Estimator schematic



$$\tilde{C}_\ell^{TT} \approx \ell^2 C_\ell^{\phi\phi} \left\langle |\nabla T|^2 \right\rangle$$

$$\underbrace{T_{\text{RMS}}^2}_{\text{Y-axis}} = \int_{\ell_{\text{min}}}^{\ell_{\text{max}}} \ell \tilde{C}_\ell^{TT} d\ell \approx \underbrace{\left\langle |\nabla T|^2 \right\rangle}_{\text{X-axis}} \underbrace{\int_{\ell_{\text{min}}}^{\ell_{\text{max}}} \ell^3 C_\ell^{\phi\phi} d\ell}_{\text{Slope}}$$

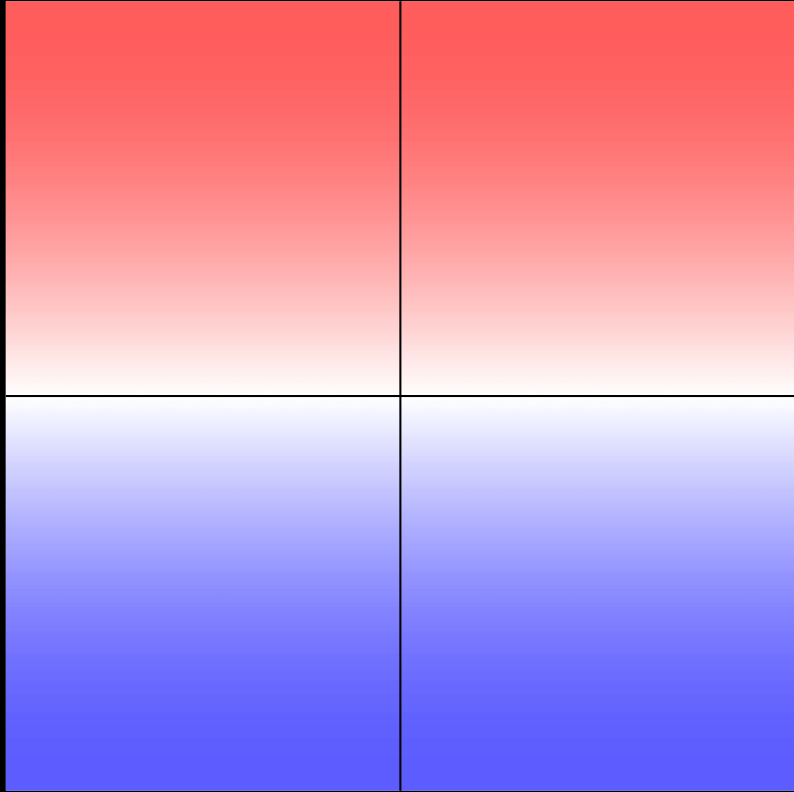
Choosing patches

T

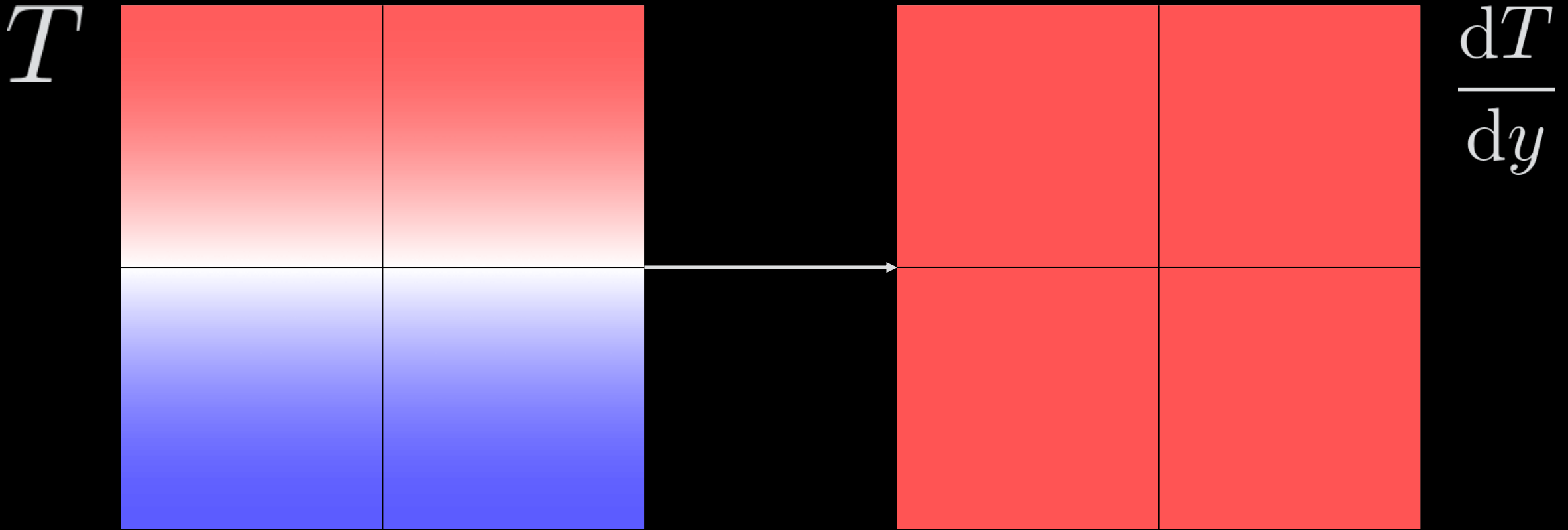


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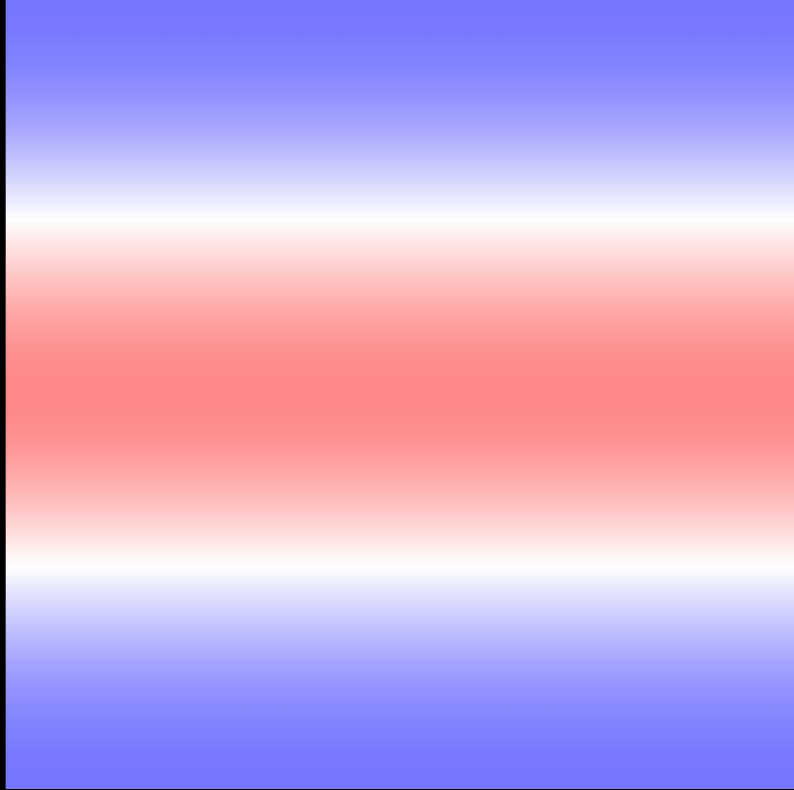


Choosing patches



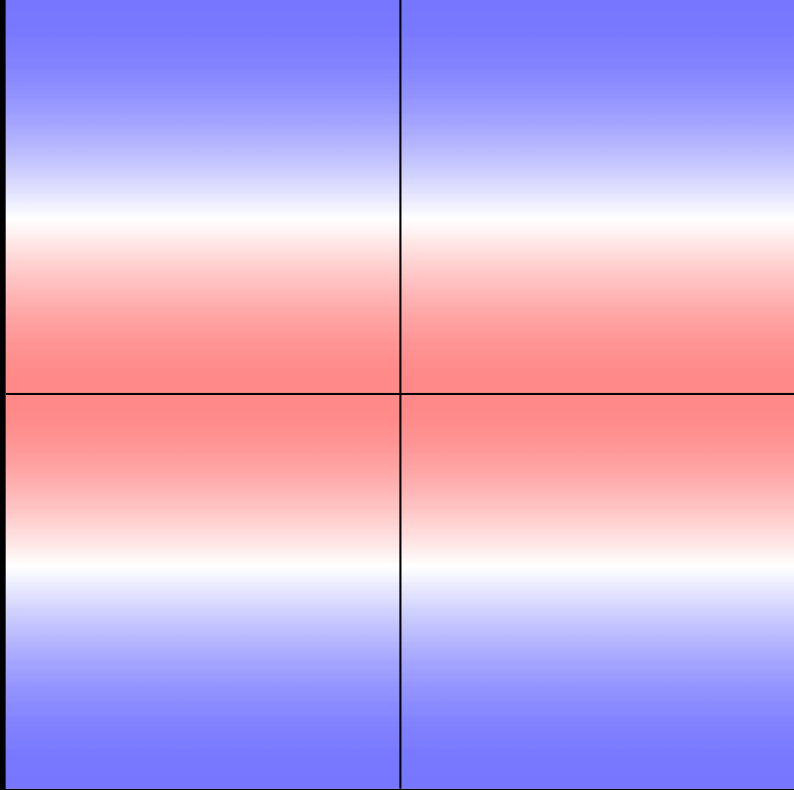
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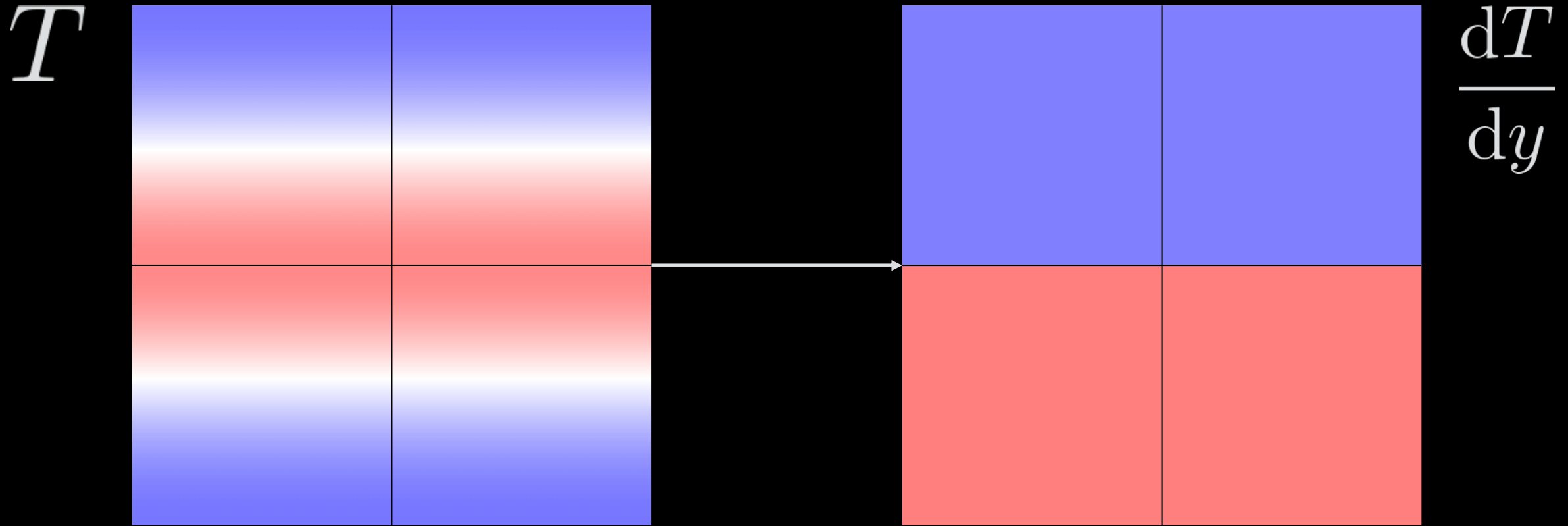


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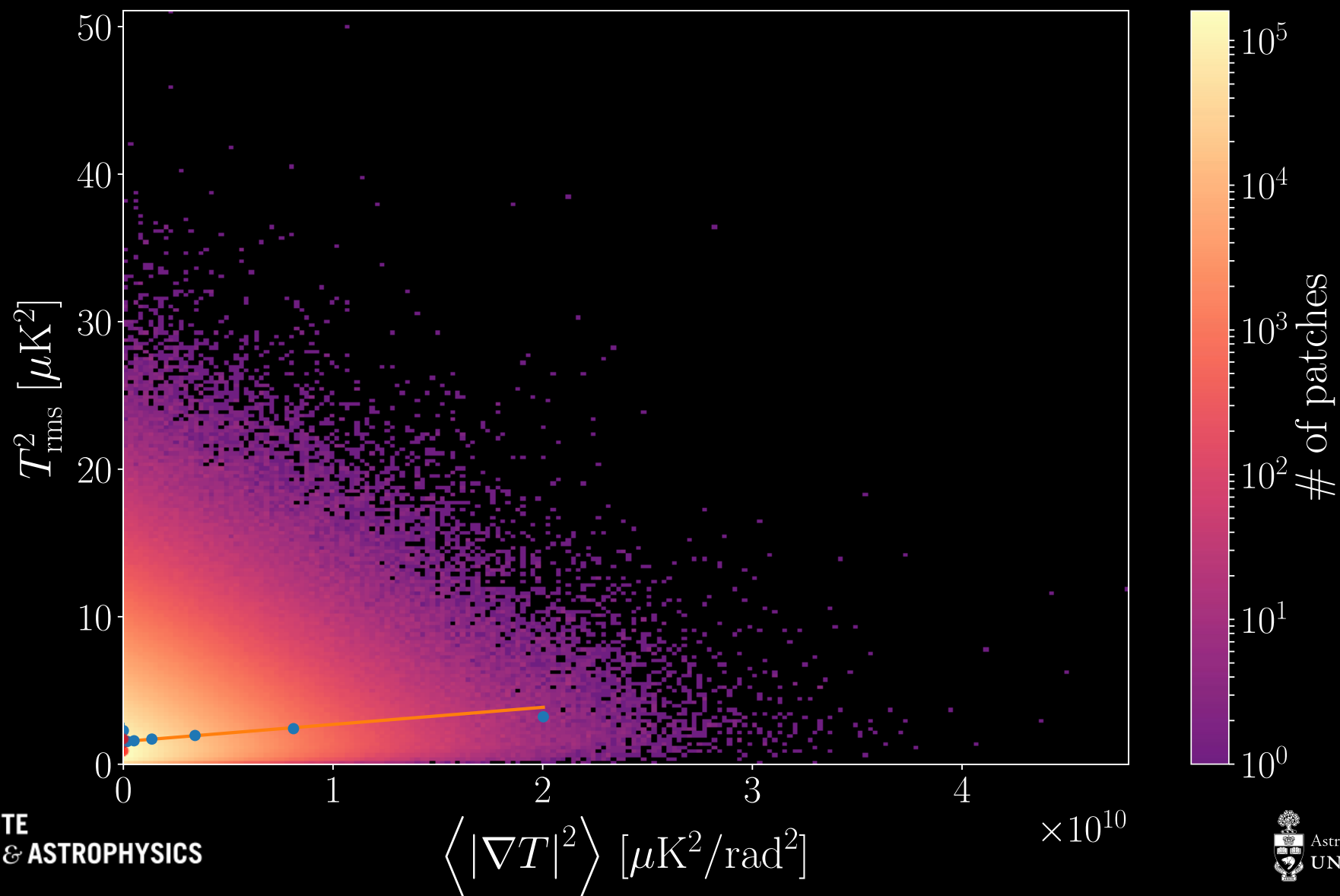
T



Choosing patches



Lensed patch-patch matching



Unlensed patch-patch matching

